Beyond Sample Equilibrium Computation



Several Questions

- Given a game *G*, does there exist a unique equilibrium in *G*?
- Given a game *G*, does there exist a strictly Pareto efficient equilibrium in *G*?
- Given a game *G* and a value *v*, does there exist an equilibrium in *G* in which some player *i* obtains an expected payoff of at least *v*?



Several Questions

- Given a game *G*, does there exist an equilibrium in which the sum of agents' utilities is at least *k*?
- Given a game G and an action a_i, does there exist an equilibrium of G in which player *i* plays action a_i with positive probability? Same question, but with probability 0?



Hardness results

- All of the above questions are NP-hard when applied to Nash equilibria.
- Even for 2-player games
- Further, guaranteed payoff and social welfare problems cannot be approximated to any constant factor in poly. time



Hardness results

• Computing all equilibria of a 2-player, general-sum game requires worst-case that is exponential in the number of actions for each player

